```
N = 65 = 5 * 13
By the Ibukiyama-Kitayama dimension formula,
dim(S_4(K(65))) = 13
By the Skoruppa-Zagier dimension formula and Jacobi restriction,
the lift dimension of S 4(K(65))^+ is 10
 the nonlift dimension of S 4(K(65))^+ is heuristically 3
 dim(S_4(K(65))^+) thus is heuristically 13
dim(S_4(K(65))^-) is heuristically 0
The heuristic dimensions are correct by the spanning results to follow
dim(J_{2,65}^{cusp}) = 1 (Skoruppa-Zagier), so need to span completely
q = 7 for TraceDown
After TD(Grit(J_{4,455})^{cusp})) and (Grit(J_{2,65})^{cusp}))^2,
 spanned rank in S_4(K(65))^+ is 13
 spanned rank in S_4(K(65))^- is 0
```

```
Final spanned rank in S_4(K(65))^- is 0 S_2(K(65)) is determined by Jacobi restriction and the H4Nd1(1) test (\dim(H_4(65,1,1)) <= 1 and this is less than \dim(J_{2,65}^{(65)}(cusp)) + 1 = 2)
```

Final spanned rank in $S_4(K(65))^+$ is 13

So $S_2(K(65)) = Grit(J_{2,65}^{cusp}) (dimension 1)$