

$$N = 247 = 13 \cdot 19$$

By the Ibukiyama-Kitayama dimension formula,
 $\dim(S_4(K(247))) = 137$

By the Skoruppa-Zagier dimension formula and Jacobi restriction,
the lift dimension of $S_4(K(247))^+$ is 47
the nonlift dimension of $S_4(K(247))^+$ is heuristically 77
 $\dim(S_4(K(247))^+)$ thus is heuristically 124
 $\dim(S_4(K(247))^-)$ is heuristically 13

$\dim(J_{\{2,247\}}^{\{\text{cusp}\}}) = 7$ (Skoruppa-Zagier), so need to span to within 6 dimensions

$q = 5$ for TraceDown

After TD($\text{Grit}(J_{\{4,1235\}}^{\{\text{cusp}\}})$) and $(\text{Grit}(J_{\{2,247\}}^{\{\text{cusp}\}}))^2$,
spanned rank in $S_4(K(247))^+$ is 124
spanned rank in $S_4(K(247))^-$ is 0

After Borcherds products,
spanned rank in $S_4(K(247))^-$ is 7

Final spanned rank in $S_4(K(247))^+$ is 124

Final spanned rank in $S_4(K(247))^-$ is 7

 $S_2(K(247))^+$ is determined by Jacobi restriction and the $H4Ndl(3,+)$ test
($\dim(H_4(247,3,1))^+ \leq 6$ and this is less than $\dim(J_{\{2,247\}}^{\{\text{cusp}\}})+1 = 8$)
 $S_2(K(247))^- = 0$ by Jacobi restriction and the $H4Ndl(1,-)$ test
($\dim(H_4(247,1,1))^- \leq 6$ and this is less than $\dim(J_{\{2,247\}}^{\{\text{cusp}\}}) = 7$)

So $S_2(K(247)) = \text{Grit}(J_{\{2,247\}}^{\{\text{cusp}\}})$ (dimension 7)