

$N = 158 = 2 \cdot 79$

By the Ibukiyama-Kitayama dimension formula,
 $\dim(S_4(K(158))) = 64$

By the Skoruppa-Zagier dimension formula and Jacobi restriction,
the lift dimension of $S_4(K(158))^+$ is 28
the nonlift dimension of $S_4(K(158))^+$ is heuristically 26
 $\dim(S_4(K(158))^+)$ thus is heuristically 54
 $\dim(S_4(K(158))^-)$ is heuristically 10

The heuristic dimensions are correct by the spanning results to follow

$\dim(J_{\{2,158\}}^{\{\text{cusp}\}}) = 3$ (Skoruppa-Zagier), so need to span to within 2 dimensions

$q = 5$ for TraceDown

After TD($\text{Grit}(J_{\{4,790\}}^{\{\text{cusp}\}})$) and $(\text{Grit}(J_{\{2,158\}}^{\{\text{cusp}\}}))^2$,
spanned rank in $S_4(K(158))^+$ is 54
spanned rank in $S_4(K(158))^-$ is 0

Hecke operators applied: $\{\{2, 2\}, \{2, 2\}, \{2, 1\}\}$

After Hecke spreading,
spanned rank in $S_4(K(158))^-$ is 8

After Borcherds products,
spanned rank in $S_4(K(158))^-$ is 10

Final spanned rank in $S_4(K(158))^+$ is 54

Final spanned rank in $S_4(K(158))^-$ is 10

$S_2(K(158))$ is determined by Jacobi restriction and the $H4Ndd(2,+)$ test
($H_4(158,2,2)^+ = 0$)

So $S_2(K(158)) = \text{Grit}(J_{\{2,158\}}^{\{\text{cusp}\}})$ (dimension 3)