

$$N = 143 = 11 \cdot 13$$

By the Ibukiyama-Kitayama dimension formula,
 $\dim(S_4(K(143))) = 44$

By the Skoruppa-Zagier dimension formula and Jacobi restriction,
the lift dimension of $S_4(K(143))^+$ is 23
the nonlift dimension of $S_4(K(143))^+$ is heuristically 17
 $\dim(S_4(K(143))^+)$ thus is heuristically 40
 $\dim(S_4(K(143))^-)$ is heuristically 4

The heuristic dimensions are correct by the spanning results to follow

$\dim(J_{\{2,143\}}^{\{\text{cusp}\}}) = 1$ (Skoruppa-Zagier), so need to span completely

$q = 5$ for TraceDown

After TD($\text{Grit}(J_{\{4,715\}}^{\{\text{cusp}\}})$) and $(\text{Grit}(J_{\{2,143\}}^{\{\text{cusp}\}}))^2$,
spanned rank in $S_4(K(143))^+$ is 40
spanned rank in $S_4(K(143))^-$ is 0

After Borcherds products,
spanned rank in $S_4(K(143))^-$ is 4

Final spanned rank in $S_4(K(143))^+$ is 40

Final spanned rank in $S_4(K(143))^-$ is 4

 $S_2(K(143))^+$ is determined by Jacobi restriction and the $H4Ndl(1,+)$ test
($\dim(H_4(143,1,1))^+ \leq 1$ and this is less than $\dim(J_{\{2,143\}}^{\{\text{cusp}\}})+1 = 2$)
 $S_2(K(143))^- = 0$ by Jacobi restriction and the $H4Ndl(1,-)$ test
($\dim(H_4(143,1,1))^- \leq 0$ and this is less than $\dim(J_{\{2,143\}}^{\{\text{cusp}\}}) = 1$)

So $S_2(K(143)) = \text{Grit}(J_{\{2,143\}}^{\{\text{cusp}\}})$ (dimension 1)