

$$N = 118 = 2 \cdot 59$$

By the Ibukiyama-Kitayama dimension formula,
 $\dim(S_4(K(118))) = 41$

By the Skoruppa-Zagier dimension formula and Jacobi restriction,
the lift dimension of $S_4(K(118))^+$ is 20
the nonlift dimension of $S_4(K(118))^+$ is heuristically 18
 $\dim(S_4(K(118))^+)$ thus is heuristically 38
 $\dim(S_4(K(118))^-)$ is heuristically 3

The heuristic dimensions are correct by the spanning results to follow

$\dim(J_{\{2,118\}}^{\{\text{cusp}\}}) = 1$ (Skoruppa-Zagier), so need to span completely

$q = 5$ for TraceDown

After TD($\text{Grit}(J_{\{4,590\}}^{\{\text{cusp}\}})$) and $(\text{Grit}(J_{\{2,118\}}^{\{\text{cusp}\}}))^2$,
spanned rank in $S_4(K(118))^+$ is 38
spanned rank in $S_4(K(118))^-$ is 0

After Borcherds products,
spanned rank in $S_4(K(118))^-$ is 3

Final spanned rank in $S_4(K(118))^+$ is 38

Final spanned rank in $S_4(K(118))^-$ is 3

 $S_2(K(118))^+$ is determined by Jacobi restriction and the $H4Nd1(1,+)$ test
($\dim(H_4(118,1,1))^+ \leq 1$ and this is less than $\dim(J_{\{2,118\}}^{\{\text{cusp}\}})+1 = 2$)
 $S_2(K(118))^- = 0$ by Jacobi restriction and the $H4Nd1(1,-)$ test
($\dim(H_4(118,1,1))^- \leq 0$ and this is less than $\dim(J_{\{2,118\}}^{\{\text{cusp}\}}) = 1$)

So $S_2(K(118)) = \text{Grit}(J_{\{2,118\}}^{\{\text{cusp}\}})$ (dimension 1)